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Article

Portfolio Optimisation in the Digital Economy: A Treynor–Black Approach

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Abstract

Digital transformation is reshaping industries, business models, and investment opportunities, creating new challenges for international portfolio management. The European communication services sector has become a strategic component of the digital economy, driven by advances in artificial intelligence (AI), digital platforms, 5G infrastructure, cloud computing, cybersecurity, and data-driven business models. Despite its importance, limited evidence exists regarding the effectiveness of portfolio optimisation strategies within digitally transforming sectors. This study investigates international portfolio optimisation using constituent firms of the MSCI Europe Communication Services 35/20 Capped Index. Drawing upon Modern Portfolio Theory and the Treynor–Black framework, an actively managed portfolio is constructed and evaluated against the SPDR® MSCI Europe Communication Services UCITS ETF and an equal-weight portfolio. Using daily market data, the analysis estimates asset returns, alpha and beta coefficients, portfolio weights, and risk-adjusted performance measures, including the Sharpe and Treynor ratios. Paired-samples *t*-tests are employed to assess the statistical significance of performance differences among investment strategies. The findings show that the Treynor–Black portfolio generated the highest annual return (27.32%), outperforming both the benchmark and equal-weight portfolios, and the highest percentage of Sharpe ratios (1.2159), suggesting that diversification benefits outweighed the advantages of active security selection. Hypothesis testing indicates no statistically significant difference between the Treynor–Black and equal-weight portfolios, and no statistically significant difference exists between the proposed and benchmark portfolios. The study extends the international portfolio management literature by applying the Treynor–Black model to a digitally transforming sector. The findings suggest that portfolio performance is influenced not only by firm-level financial characteristics but also by broader digital and institutional environments. Firms operating within digitally advanced and well-governed economies appear better positioned to exploit technological innovation and generate sustainable long-term value. Overall, the results demonstrate that successful international portfolio optimization requires balancing active security selection with diversification while recognizing the role of digital transformation, governance quality, and innovation ecosystems in shaping investment performance within the digital economy.



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1. Introduction

The global economy is undergoing profound transformation driven by digitalisation, technological disruption, geopolitical uncertainty, and evolving regulatory priorities. The cascading effects of COVID-19, climate change, geopolitical instability, and rising economic nationalism have exposed structural weaknesses in existing governance, financial, and economic systems, challenging their capacity to ensure resilience and long-term sustainability (Alkaraan & Hussainey, 2025). These challenges are further reinforced by the growing complexity of global risks associated with technological acceleration, geostrategic shifts, climate change, demographic transitions, political polarisation, trade tensions, and declining institutional trust. According to the World Economic Forum’s Global Risks Report 2025, existing governance frameworks appear increasingly ill-equipped to address both emerging and interconnected global risks, contributing to greater uncertainty and fragility across economic and financial systems (WEF, 2025).

At the same time, governments and businesses are accelerating investments in artificial intelligence (AI), cloud computing, cybersecurity, advanced telecommunications infrastructure, and digital platforms, while initiatives such as the European Union’s Digital Decade Strategy seek to strengthen digital capabilities, innovation ecosystems, and international competitiveness (Teixeira & Tavares-Lehmann, 2022; Sadeghi et al., 2024). These developments are reshaping financial markets and investment decision-making as technological capability, innovation capacity, and digital infrastructure increasingly complement traditional sources of competitive advantage (Feng et al., 2024). However, rapid technological change also introduces new forms of uncertainty, increasing the importance of portfolio optimisation and risk management. In this context, digital and behavioural indicators can provide valuable insights into market dynamics, with digital attention measures serving as early warning signals of volatility and supporting more effective forecasting and investment decisions (Lababidi et al., 2026). Evidence from the Eurozone suggests that, while highly rated ESG firms do not consistently outperform lower-rated firms under all market conditions, their performance improves significantly in countries characterised by stronger governance quality, highlighting the importance of institutional effectiveness in enhancing investment outcomes and portfolio resilience (Asteriou et al., 2024).

The communication services sector provides a valuable setting for examining these developments within the digital economy. Once centred on telecommunications and traditional media, it has evolved into a digital ecosystem encompassing online platforms, streaming services, cloud communications, artificial intelligence applications, and advanced connectivity services. Through investments in 5G, cybersecurity, cloud technologies, and AI-enabled solutions, firms in the sector play a central role in Europe’s digital transformation. Despite its strategic importance, portfolio management research provides limited evidence on portfolio optimisation within these innovation-intensive sectors. Most studies focus on broad market indices and diversification strategies, overlooking how digital transformation may reshape risk-return relationships through its effects on innovation capability, competitive positioning, growth opportunities, and firm performance. This oversight creates a significant gap for active portfolio management strategies, such as the Treynor–Black framework, which are predicated on identifying mispriced securities driven by firm-specific factors.

A second limitation concerns the limited integration between the digital transformation and international portfolio management literature. Prior research shows that Industry 4.0 technologies enhance organisational performance and sustainable competitive advantage, while governance quality strengthens firms' ability to convert technological investments into long-term value creation. More recent studies highlight the complementary roles of governance, innovation, and sustainability in improving organisational resilience, competitiveness, ESG performance, and financial outcomes. Similarly, AI-enabled Industry 4.0 technologies have been shown to accelerate innovation, digital integration, and ecosystem value creation when supported by effective governance structures (Alkaraan et al., 2026). Digital transformation also enhances organisational agility and resilience (Probojakti et al., 2025), while innovation capability strengthens the contribution of leadership and knowledge resources to organisational performance (Harsono et al., 2025). However, despite these advances, limited attention has been devoted to understanding how these drivers of digital economy performance—specifically digital transformation, governance quality, innovation capability, and institutional effectiveness—influence the inputs and efficacy of active portfolio construction models. Consequently, an important theoretical and empirical gap remains at the intersection of international portfolio optimisation, the digital economy, and active investment performance.

A third limitation relates to the application of the Treynor–Black active portfolio optimisation model, in particular, within digitally transforming and innovation-intensive sectors. Although the Treynor–Black model remains one of the most influential active portfolio management frameworks for exploiting security-specific mispricing, empirical applications have largely focused on broad market portfolios and traditional industries, with limited evidence regarding its effectiveness within the European communication services sector. This gap is particularly important for a digital economy study because firms in the sector operate across countries characterised by varying levels of digital maturity, governance quality, institutional effectiveness, innovation capacity, and regulatory sophistication. Such differences may influence the very signals (i.e., alpha forecasts) and risk characteristics that the Treynor–Black model relies upon, thereby affecting portfolio performance and investment outcomes. Moreover, effective governance structures play a critical role in supporting strategic transformation and sustainable value creation by strengthening internal and external control mechanisms and enhancing organisational adaptability.

To address these limitations and contribute to the literature on portfolio optimisation in the digital economy, this study focuses on the MSCI Europe Communication Services 35/20 Capped Index and applies the Treynor–Black optimisation framework. The objective is to determine whether active portfolio management can generate superior risk-adjusted returns within this unique digital context. Specifically, the study evaluates the Treynor–Black portfolio's performance against both a passive benchmark and a naïve diversification strategy to assess the value added by active security selection. Accordingly, the study addresses the following research questions

RQ1: Can a Treynor–Black optimised portfolio outperform the MSCI Europe Communication Services benchmark?

RQ2: Is there a significant performance difference between a Treynor–Black portfolio and an equal-weight portfolio in the European communication services sector?

RQ3: To what extent does active portfolio optimisation create value in a digitally transforming sector?

To address these questions, the study tests the following hypotheses:

H1. *There is no statistically significant difference between the performance of the Treynor–Black portfolio and the equal-weight portfolio.*

H2. *There is no statistically significant difference between the performance of the Treynor–Black portfolio and the benchmark MSCI Europe Communication Services market portfolio.*

This study contributes to the literature in four important ways. First, it extends international portfolio management research by examining portfolio optimisation within a strategically important sector at the centre of Europe’s digital transformation agenda. Second, it bridges the gap between portfolio management and digital transformation research by exploring how digital maturity, governance quality, innovation capability, and institutional effectiveness may influence portfolio-level outcomes. Third, it provides empirical evidence regarding the effectiveness of the Treynor–Black model within a contemporary international investment setting. Finally, the study offers practical insights for investors, fund managers, and financial institutions regarding portfolio construction, security selection, diversification, and risk management within digitally transforming industries.

The remainder of the paper is organised as follows. Section 2 reviews the relevant literature and theoretical foundations underpinning international portfolio management and portfolio optimisation. Section 3 outlines the research methodology and portfolio construction framework. Section 4 presents the empirical analysis and portfolio optimisation results. Section 5 discusses the findings of this study. Finally, Section 6 concludes the study, highlights theoretical and managerial implications, identifies limitations, and proposes directions for future research.

2. Literature Review and Theoretical Framework

2.1. Theoretical Foundations of International Portfolio Optimisation

International portfolio optimisation seeks to maximise risk-adjusted returns through efficient asset allocation, diversification, and security selection. As financial markets have become increasingly integrated, investors have gained access to a broader range of investment opportunities across countries, sectors, and asset classes. Consequently, effective portfolio management requires balancing return generation with risk control in increasingly complex and interconnected market environments.

The foundations of portfolio optimisation originate from Modern Portfolio Theory (MPT), developed by Markowitz (1952). MPT demonstrates that investors can improve portfolio efficiency by combining imperfectly correlated assets, thereby reducing unsystematic risk without necessarily sacrificing expected returns. This principle gave rise to the efficient frontier, which identifies portfolios offering the highest expected return for a given level of risk.

Building upon MPT, the Capital Asset Pricing Model (CAPM), developed by Sharpe (1964), Lintner (1965), and Mossin (1966), explains the relationship between expected returns and systematic risk. CAPM distinguishes between systematic risk, which cannot be eliminated through diversification, and unsystematic risk, which can be diversified away. The model proposes that investors are compensated only for systematic risk, measured by beta, and provides the theoretical basis for estimating abnormal returns (alpha), a central concept in active portfolio management.

The increasing integration of global financial markets has further strengthened the importance of international diversification. Diversification across countries enables investors to benefit from differences in economic conditions, institutional environments, governance systems, and growth opportunities. Because international markets are often imperfectly correlated, global diversification can reduce portfolio volatility while preserving return

potential, particularly during periods of economic uncertainty, technological disruption, and geopolitical instability.

Portfolio management strategies are generally classified as passive or active. Passive approaches seek to replicate benchmark performance through broad market exposure, often using exchange-traded funds (ETFs), whereas active approaches attempt to outperform benchmark portfolios through security selection and portfolio rebalancing. One of the most influential active portfolio management frameworks is the Treynor–Black model (Treynor & Black, 1973), which combines active security selection with passive market exposure. The model allocates capital according to expected abnormal returns and residual risk, thereby seeking to maximise risk-adjusted performance.

The Treynor–Black framework is particularly relevant in sectors characterised by rapid technological change, innovation intensity, and potential market inefficiencies, where firm-specific differences may create opportunities for superior returns. Collectively, MPT, CAPM, international diversification theory, and the Treynor–Black model provide the financial foundations for this study. However, these theories were largely developed before the emergence of the digital economy and therefore provide limited insight into how digital transformation, governance quality, innovation capability, and institutional effectiveness may influence investment opportunities and portfolio performance.

2.2. Digital Transformation, Governance, and Investment Performance: Conceptual Framework and Research Gap

Digital transformation has emerged as a major driver of innovation, competitiveness, and long-term value creation. Advances in artificial intelligence, cloud computing, big data analytics, digital platforms, telecommunications infrastructure, and Industry 4.0 technologies have fundamentally reshaped business models, organisational processes, and sources of competitive advantage across industries. Within the communication services sector, these developments have accelerated the convergence of telecommunications, media, and digital services, creating new growth opportunities while increasing technological complexity and competitive pressures. Prior research demonstrates that digital transformation enhances organisational performance and sustainable competitive advantage. In particular, AI, cloud solutions, mobile accounting, and robotic process automation support business continuity, remote working, and operational efficiency, while AI-enabled Industry 4.0 technologies accelerate innovation, digital integration, ESG performance, and ecosystem value creation (Alkaraan et al., 2026). Beyond operational benefits, digital transformation increasingly shapes firms' strategic positioning, growth prospects, and long-term value creation.

The ability of organisations to realise these benefits, however, depends significantly on governance quality, leadership capabilities, and institutional effectiveness. Digital transformation strengthens organisational agility and resilience, enabling firms to respond more effectively to technological disruption and changing market conditions (Probojakti et al., 2025). Likewise, the integration of governance structures, innovation strategies, sustainability practices, and digital technologies enhances organisational competitiveness, resilience, and financial performance. Effective governance mechanisms facilitate the conversion of technological investments into innovation outcomes and sustainable value creation, while transformational leadership and knowledge management strengthen innovation capability and organisational effectiveness (Harsono et al., 2025). Similar evidence from the financial sector shows that FinTech adoption improves operational efficiency and organisational performance, highlighting the strategic importance of technological innovation in enhancing competitiveness and value creation (Goel & Kashiramka, 2025). Collectively, these findings suggest that firms operating within digitally mature and institutionally robust environments are better positioned to sustain innovation, strengthen resilience, and generate long-term value.

These developments also have important implications for investors and portfolio managers. Drawing on portfolio optimisation theory, this study argues that differences in digital maturity, governance quality, innovation capability, ESG performance, and institutional effectiveness may influence portfolio outcomes through their effects on firm growth, competitive positioning, resilience, and risk–return characteristics. Firms operating within advanced digital ecosystems and supported by strong governance frameworks are therefore expected to exhibit greater abnormal return potential and stronger investment attractiveness. This argument is reinforced by evidence showing that high-quality external governance mechanisms, such as Big Four audit assurance, reduce the gap between corporate sustainability performance and disclosure practices, thereby improving the credibility and reliability of non-financial reporting. Consequently, digital transformation and governance quality should be viewed not only as organisational capabilities but also as strategic factors that influence investment opportunities, portfolio construction, and long-term portfolio performance.

Despite growing interest in digital transformation, governance, and sustainability, important gaps remain in the literature. Portfolio optimisation research has devoted limited attention to sectors experiencing rapid technological change, while empirical applications of the Treynor–Black framework within the European communication services sector remain scarce. Furthermore, limited evidence exists regarding whether actively managed portfolios can outperform benchmark ETFs and equal-weight portfolios in innovation-intensive industries characterised by heterogeneous risk–return profiles. Although prior studies establish important links between digital transformation, governance quality, ESG performance, and organisational outcomes, considerably less is known about how these factors influence portfolio construction, security selection, and investment performance. This limitation is increasingly important as digital capabilities, governance effectiveness, ESG performance, audit quality, and institutional factors become critical determinants of long-term value creation and investment attractiveness.

Accordingly, this study positions international portfolio optimisation at the intersection of portfolio management, digital transformation, governance, innovation, sustainability, and FinTech research. It addresses an important theoretical and empirical gap by examining whether active portfolio optimisation can generate superior risk-adjusted returns within the European communication services sector, a sector positioned at the forefront of digital transformation, innovation-led growth, and technological change. In doing so, the study extends the portfolio management literature by incorporating broader digital, governance, ESG, and institutional dimensions into the analysis of investment performance and portfolio optimisation.

3. Methodology

3.1. Research Design and Data Collection

This study adopts a quantitative research design to examine international portfolio optimisation within the European communication services sector. The analysis relies on historical financial market data to estimate risk–return relationships, construct optimised portfolios, evaluate performance, and test hypotheses using established financial models and statistical techniques.

The study is grounded in Modern Portfolio Theory (Markowitz, 1952), the Capital Asset Pricing Model (CAPM) (Sharpe, 1964; Lintner, 1965; Mossin, 1966), and the Treynor–Black portfolio optimisation framework (Treynor & Black, 1973). These theories provide the foundation for assessing whether active portfolio management can generate superior risk-adjusted returns relative to passive investment strategies.

The sample comprises all firms included in the MSCI Europe Communication Services 35/20 Capped Index, covering telecommunications services, digital platforms, media and entertainment, communication infrastructure, online marketplaces, advertising services, and digital content distribution. The SPDR[®] MSCI Europe Communication Services UCITS ETF is used as the benchmark market portfolio because it closely replicates the performance of the underlying index and serves as both the market portfolio for the Treynor–Black model and the benchmark for performance evaluation.

The empirical analysis is based on secondary financial data obtained from recognised financial databases and publicly available market sources, such as European Stock Market-Investing.com (<https://www.investing.com/equities/europe>, accessed on 8–15 October 2025). The dataset includes daily stock prices, ETF prices, market returns, and risk-free rate data. The study period is divided into two phases. The portfolio formation period (9 January 2024–30 December 2024) is used to estimate portfolio optimisation parameters, while the portfolio evaluation period (6 January 2025–7 October 2025) is used to assess out-of-sample portfolio performance. This separation reduces the risk of overfitting and strengthens the robustness of the analysis.

3.2. Portfolio Optimisation Framework

Portfolio construction follows the Treynor–Black optimisation framework, which combines active security selection with passive market exposure. The model assumes that investors can identify securities capable of generating abnormal returns while maintaining the diversification benefits associated with market investment.

The optimisation procedure consists of four stages. First, daily returns are calculated for all constituent firms and the benchmark ETF. Second, beta coefficients, alpha values, and residual variances are estimated using the market model. Third, securities exhibiting favourable alpha-risk characteristics are selected for inclusion in the active portfolio. Finally, portfolio weights are determined according to the Treynor–Black allocation procedure, whereby capital is allocated according to the relationship between abnormal return and residual risk.

The final portfolio combines the actively managed portfolio with the benchmark ETF to maximise risk-adjusted returns while maintaining diversification and controlling firm-specific risk.

3.3. Portfolio Performance Evaluation and Hypothesis Testing

The proposed portfolio is evaluated against two alternative investment strategies: (1) the benchmark SPDR[®] MSCI Europe Communication Services UCITS ETF and (2) an equal-weight portfolio. This comparison enables an assessment of whether active portfolio optimisation provides additional value beyond passive investment and simple diversification strategies.

Portfolio performance is assessed using return and risk-adjusted measures, including portfolio return, beta, standard deviation, Sharpe ratio, Treynor ratio, and Jensen’s alpha. These measures evaluate profitability, risk exposure, diversification efficiency, and the value added through active management.

The following hypotheses are tested:

H1. *There is no statistically significant difference between the risk-adjusted performance of the Treynor–Black portfolio and the equal-weight portfolio.*

H2. *There is no statistically significant difference between the risk-adjusted performance of the Treynor–Black portfolio and the benchmark ETF portfolio.*

Paired-samples *t*-tests are conducted using daily portfolio returns during the evaluation period to determine whether statistically significant differences exist between portfolio strategies.

3.4. Data Analysis Techniques

The empirical analysis is conducted using SPSS 19.0. Excel is used for data preparation, return calculations, portfolio optimisation, and performance measurement, while SPSS is employed for statistical analysis and hypothesis testing. The analytical procedures include descriptive statistics, risk-return analysis, beta and alpha estimation, portfolio optimisation, performance comparison, paired-samples *t*-test, and statistical significance testing. These techniques enable a rigorous evaluation of whether the proposed Treynor–Black portfolio outperforms the equal-weight portfolio and the benchmark ETF.

By integrating portfolio optimisation techniques with statistical testing, the study provides empirical evidence on the effectiveness of active portfolio management within a sector characterised by digital transformation, technological innovation, and evolving governance environments.

4. Empirical Analysis and Portfolio Optimisation Results

This section presents the empirical implementation of the proposed international portfolio optimisation framework using constituent firms included in the MSCI Europe Communication Services 35/20 Capped Index. Consistent with the study's objectives, the analysis evaluates whether active portfolio optimisation can generate superior investment performance relative to passive benchmark strategies within a sector undergoing significant digital transformation and technological change. The empirical analysis proceeds through six stages. First, the benchmark portfolio and sector characteristics are examined. Second, the return and risk characteristics of constituent firms are analysed. Third, securities are screened using systematic risk (beta) and abnormal return (alpha) measures. Fourth, the Treynor–Black optimisation model is applied to construct the active portfolio. Fifth, portfolio performance is evaluated using established risk-adjusted performance measures. Finally, statistical hypothesis testing is conducted to compare the proposed portfolio against alternative investment strategies.

4.1. Benchmark Portfolio and Sector Characteristics

4.1.1. Benchmark Portfolio Selection

The European communication services sector has undergone substantial transformation over the past decade, evolving from a traditional telecommunications and media industry into a digitally enabled ecosystem encompassing online platforms, streaming services, digital advertising, cloud communications, artificial intelligence applications, and advanced connectivity solutions. As a result, the sector has become a key enabler of Europe's digital economy, supporting technological innovation, digital infrastructure development, and innovation-led growth. To capture the performance of this rapidly evolving sector, this study employs the MSCI Europe Communication Services 35/20 Capped Index, a widely recognised benchmark comprising large- and mid-cap communication services companies across 15 developed European markets. Figure 1 shows constituent companies and portfolio weights of the MSCI Europe Communication Services ETF.

To provide a benchmark for portfolio construction and performance evaluation, the study employs the SPDR® MSCI Europe Communication Services UCITS ETF. The ETF closely tracks the MSCI Europe Communication Services 35/20 Capped Index and provides diversified exposure to 23 constituent companies operating across telecommunications, digital media, entertainment, advertising, online marketplaces, communication infrastruc-

ture, and related technology-enabled services. Managed by State Street Global Advisors Europe Limited and domiciled in Ireland under the UCITS regulatory framework, the ETF adopts a full physical replication strategy, thereby minimising tracking error and ensuring close alignment with the underlying index. Within this study, the ETF serves two important functions: first, as the market portfolio required for implementing the Treynor–Black optimisation model; and second, as the benchmark against which the performance of the proposed actively managed portfolio is evaluated. Consequently, it provides a robust and realistic reference point for assessing whether active portfolio optimisation can generate superior risk-adjusted returns relative to a passive investment strategy (Table 1). Figure 2 shows cumulative performance and benchmark portfolio characteristics of the MSCI Europe Communication Services 35/20 Capped Index and SPDR® MSCI Europe Communication Services UCITS ETF (May 2011–May 2026).

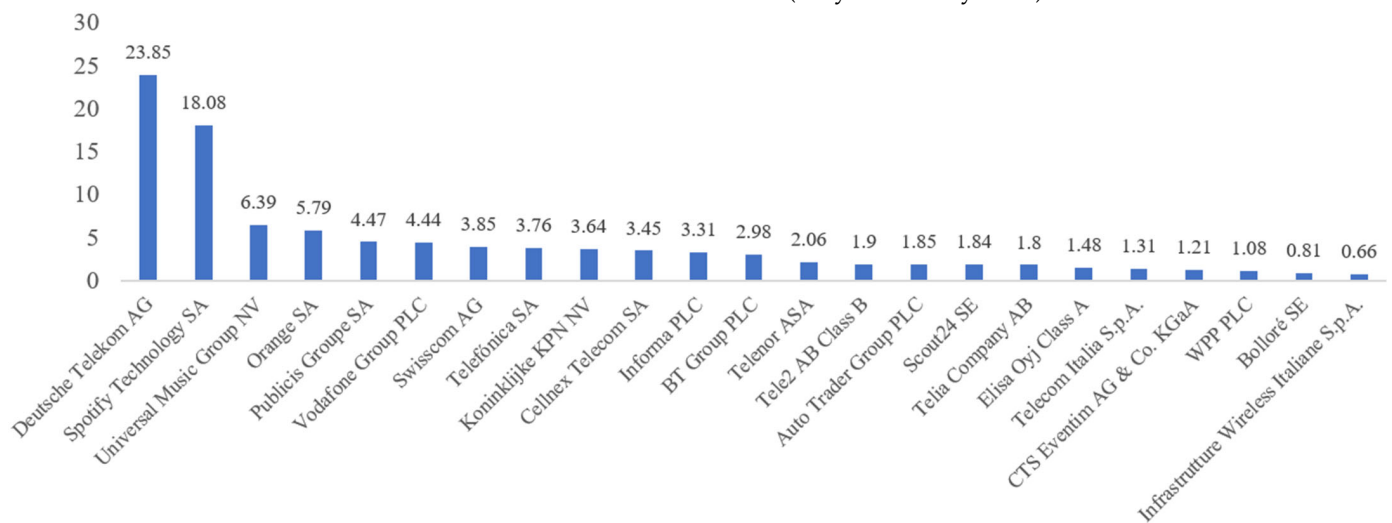


Figure 1. Constituent companies and portfolio weights of the MSCI Europe Communication Services ETF.

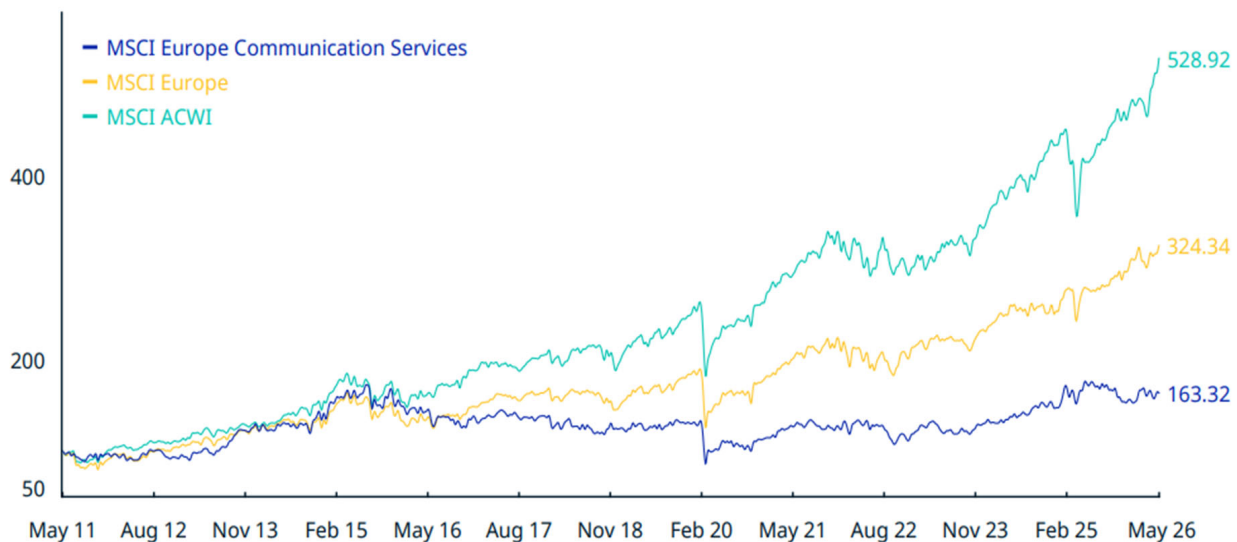


Figure 2. Cumulative performance and benchmark portfolio characteristics of the MSCI Europe Communication Services 35/20 Capped Index and SPDR® MSCI Europe Communication Services UCITS ETF (May 2011–May 2026). Source: State Street Global Advisors (SPDR ETFs) and MSCI Europe Communication Services Index (EUR) (2025).

Table 1. Key Characteristics of the SPDR® MSCI Europe Communication Services UCITS.

Characteristics	Description
Full Fund Name	SPDR® MSCI Europe Communication Services UCITS ETF
Benchmark Index	MSCI Europe Communication Services 35/20 Capped Index
Fund Manager	State Street Global Advisors Europe Limited
Launch Date	5 December 2014
Domicile	Ireland
Assets Under Management (AUM)	€203.39 million (October 2025)
Number of Holdings	23 constituent companies
Replication Method	Full Physical Replication
Regulatory Framework	Undertakings for Collective Investment in Transferable Securities (UCITS)

Source: State Street Global Advisors (SPDR ETFs) and [MSCI Europe Communication Services Index \(EUR\) \(2025\)](#).

4.1.2. Portfolio Composition and Sector Characteristics

The constituent firms and portfolio weightings of the benchmark ETF are presented in Figure 1. The portfolio comprises 23 leading European communication services companies operating across telecommunications, digital media, entertainment, advertising, online marketplaces, communication infrastructure, and related technology-enabled services. As such, the ETF provides diversified exposure to the principal segments of the modern European communication services sector.

Figure 1 indicates a relatively concentrated portfolio structure, with the ten largest holdings accounting for approximately 78% of total portfolio value. Deutsche Telekom AG and Spotify Technology SA represent the largest positions, reflecting their market leadership and strategic importance within the European communication services ecosystem. While this concentration increases exposure to firm-specific risk, it also reflects the dominant role of a small number of large-cap firms in shaping sector performance. Importantly, the portfolio remains diversified across a range of business models and revenue streams, including telecommunications infrastructure, digital content distribution, music streaming, online marketplaces, advertising services, and business information platforms. This diversity mirrors the growing convergence of telecommunications, technology, media, and digital services within Europe’s digital economy. From a portfolio optimisation perspective, the coexistence of mature telecommunications operators and rapidly expanding digital firms creates substantial variation in risk–return characteristics, providing a favourable setting for active portfolio management and the application of the Treynor–Black optimisation framework.

4.1.3. Geographic Diversification and Country Allocation of the Benchmark Portfolio

The geographic allocation of the benchmark portfolio provides an overview of the international diversification characteristics of the European communication services sector. As illustrated in Table 2, the ETF maintains exposure across multiple European markets while exhibiting notable concentration in four key economies: Germany, Luxembourg, the United Kingdom, and France. Together, these countries account for approximately 70.8% of total portfolio value, reflecting their dominant position within the European communication services industry.

Table 2. Geographic allocation of the SPDR® MSCI Europe Communication Services UCITS ETF.

Country	Portfolio Weight (%)
Germany	27.69
Luxembourg	18.59
United Kingdom	13.78
France	10.74
Other European Countries	29.20

Germany represents the largest country allocation, accounting for 27.69% of portfolio value, followed by Luxembourg (18.59%), the United Kingdom (13.78%), and France (10.74%). The remaining 29.20% is distributed across other European markets, including the Netherlands, Sweden, Norway, Switzerland, Spain, Finland, and Italy. This distribution provides broad exposure to the European communication services sector while reducing dependence on any single national market. From an international portfolio optimisation perspective, the geographic composition of the ETF offers diversification benefits through exposure to multiple economic and market environments. At the same time, the concentration of holdings in several leading European economies reflects their significant contribution to sector growth, market capitalisation, and investment opportunities. Consequently, the benchmark portfolio provides a suitable foundation for evaluating whether active portfolio optimisation can generate superior risk-adjusted performance relative to a diversified passive investment strategy.

4.2. Return Characteristics of Constituent Firms

The first stage of the optimisation process involves estimating the return performance of constituent securities. Daily returns are calculated using the following expression:

$$[R_{it}] = \frac{P_t - P_{t-1}}{P_{t-1}}$$

where (R_{it}) denotes the daily return of security (i), and (P_t) and (P_{t-1}) represent consecutive daily closing prices. The average return for each security is calculated as:

$$[\bar{R}_i] = \frac{\sum_{t=1}^n R_{it}}{n}$$

Table 3 presents the average daily returns of the benchmark ETF and its constituent firms during the portfolio formation period (9 January 2024–30 December 2024). The results reveal considerable variation in return performance across the sector. As shown in Table 3, Spotify Technology SA generated the highest average daily return (0.003813), followed by CTS Eventim AG & Co. KGaA (0.001391), Scout24 SE (0.001131), Deutsche Telekom AG (0.001050), and BT Group plc (0.001035). These firms substantially outperformed the benchmark ETF, which recorded an average daily return of 0.000502 during the same period. In contrast, several firms generated negative average returns, including Infrastructure Wireless Italiane S.p.A. (−0.000610), Telecom Italia S.p.A. (−0.000440), Cellnex Telecom SA (−0.000390), and Orange SA (−0.000360).

The performance differences reported in Table 3 demonstrate significant heterogeneity among firms despite their common industry classification. From a portfolio management perspective, this variation is particularly important because it suggests that investment opportunities are not evenly distributed across the sector. Consequently, investors may be able to improve portfolio outcomes through active security selection rather than relying solely on passive exposure to the benchmark index. The results therefore provide

preliminary support for the application of the Treynor–Black optimisation framework, which seeks to identify securities capable of generating superior returns relative to the market portfolio. Overall, the return dispersion observed in Table 3 provides a strong foundation for the subsequent analysis of systematic risk, abnormal returns, and portfolio optimisation opportunities.

Table 3. Average daily returns of the benchmark ETF and constituent firms during the portfolio formation period (2024).

Asset/Company	Average Daily Return	Asset/Company	Average Daily Return
SPDR® MSCI Europe Communication Services UCITS ETF (Benchmark ETF)	0.000502176	Publicis Groupe SA	0.000847
Auto Trader Group PLC	0.000619005	Scout24 SE	0.001131
Bolloré SE	0.000190318	Spotify Technology SA	0.003813
BT Group plc	0.001035084	Swisscom AG	−0.000052
Cellnex Telecom SA	−0.000390	Tele2 AB Class B	0.000982
CTS Eventim AG & Co. KGaA	0.001391	Telecom Italia S.p.A.	−0.000440
Deutsche Telekom AG	0.001050	Telefónica SA	0.000279
Elisa Oyj Class A	−0.000018	Telenor ASA	0.000255
Informa PLC	0.000405	Telia Company AB	0.000414
Infrastructure Wireless Italiane S.p.A.	−0.000610	Universal Music Group NV	0.00007861
Koninklijke KPN NV	0.000513	Vodafone Group PLC	0.0000907
Orange SA	−0.000360	WPP PLC	0.000464

Source: Author's calculations based on daily trading data for constituent firms included in the MSCI Europe Communication Services 35/20 Capped Index during the portfolio formation period (9 January 2024–30 December 2024).

4.3. Systematics Risk and Abnormal Performance Analysis

4.3.1. Beta Analysis and Systematic Risk Characteristics

Systematic risk is measured using the beta coefficient:

$$\beta_i = \frac{\text{Cov}(R_i, R_m)}{\text{Var}(R_m)}$$

where (R_i) represents the return of security (i), and (R_m) denotes the return of the market portfolio.

As shown in Table 4, Beta coefficients provide an indication of each firm's exposure to systematic risk. Securities with beta values greater than one are more sensitive to market movements and are therefore expected to experience larger gains during favourable market conditions as well as greater losses during market downturns. Conversely, beta values below one indicate lower market sensitivity and more defensive investment characteristics, while negative beta values suggest an inverse relationship with market performance. The results reveal substantial variation in systematic risk across firms included in the MSCI Europe Communication Services Index. Vodafone Group PLC recorded the highest beta coefficient ($\beta = 1.451$), followed by BT Group plc ($\beta = 1.205$), Telecom Italia S.p.A. ($\beta = 1.167$), and Auto Trader Group PLC ($\beta = 0.9745$). These firms exhibit the greatest responsiveness to market fluctuations and may offer enhanced return potential during periods of favourable market sentiment, albeit with higher levels of systematic risk.

Table 4. Beta coefficients (β) of the benchmark ETF constituents during the portfolio formation period (2024).

Asset/Company	Beta (β)	Asset/Company	Beta (β)
SPDR [®] MSCI Europe Communication Services UCITS ETF	–	Publicis Groupe SA	0.089619
Auto Trader Group PLC	0.974542	Scout24 SE	0.748554
Bolloré SE	0.448476	Spotify Technology SA	0.518134
BT Group plc	1.204983	Swisscom AG	0.479947
Cellnex Telecom SA	0.499549	Tele2 AB Class B	–0.041770
CTS Eventim AG & Co. KGaA	0.762596	Telecom Italia S.p.A.	1.166984
Deutsche Telekom AG	0.423818	Telefónica SA	0.853639
Elisa Oyj Class A	–0.075020	Telenor ASA	0.083701
Informa PLC	0.211934	Telia Company AB	0.405644
Infrastructure Wireless Italiane S.p.A.	0.243555	Universal Music Group NV	–0.127943
Koninklijke KPN NV	0.499074	Vodafone Group PLC	1.450587
Orange SA	0.732181	WPP PLC	0.256905

Source: Author's calculations based on daily trading data for constituent firms included in the MSCI Europe Communication Services 35/20 Capped Index during the portfolio formation period (9 January 2024–30 December 2024).

A second group of firms demonstrates moderate market sensitivity, including Telefónica SA ($\beta = 0.854$), CTS Eventim AG & Co. KGaA ($\beta = 0.763$), Scout24 SE ($\beta = 0.749$), Orange SA ($\beta = 0.732$), Spotify Technology SA ($\beta = 0.518$), Cellnex Telecom SA ($\beta = 0.500$), and Koninklijke KPN NV ($\beta = 0.499$). These securities provide exposure to market growth opportunities while maintaining lower levels of systematic risk than the highest-beta firms. Several firms exhibit relatively defensive characteristics, including Deutsche Telekom AG ($\beta = 0.424$), Telia Company AB ($\beta = 0.406$), WPP PLC ($\beta = 0.257$), Infrastructure Wireless Italiane S.p.A. ($\beta = 0.244$), Informa PLC ($\beta = 0.212$), Telenor ASA ($\beta = 0.084$), and Publicis Groupe SA ($\beta = 0.090$). These firms are less sensitive to market fluctuations and may contribute to portfolio stability during periods of uncertainty. Interestingly, three firms reported negative beta coefficients: Universal Music Group NV ($\beta = -0.128$), Elisa Oyj Class A ($\beta = -0.075$), and Tele2 AB Class B ($\beta = -0.042$). Although relatively small in magnitude, these coefficients suggest limited dependence on broader market movements and indicate potential diversification benefits.

The above results highlight the heterogeneous risk structure of the European communication services sector. The coexistence of high-beta growth-oriented firms, moderate-risk firms, and defensive securities creates favourable conditions for active portfolio optimisation. Such variation in systematic risk is particularly important within the Treynor–Black framework because it enables the identification of securities with different risk–return characteristics and provides the foundation for subsequent security screening and portfolio construction.

4.3.2. Alpha Analysis and Security Selection Opportunities

While beta measures a security's exposure to systematic market risk, alpha captures the component of return that cannot be explained by market movements and therefore represents abnormal performance relative to the benchmark portfolio. Within the Treynor–Black framework, alpha plays a central role in identifying securities with the potential

to outperform market expectations. Alpha coefficients were estimated using the market model as the following expression:

$$R_i = \alpha_i + \beta_i(R_m) + \varepsilon_i$$

where (α_i) denotes the abnormal return of security (i), (R_i) represents the return of the security, (β_i) is the estimated beta coefficient, and (R_m) is the return of the market portfolio. A positive alpha indicates that a security generated returns above those predicted by its level of systematic risk, whereas a negative alpha suggests underperformance relative to market expectations. Consequently, securities exhibiting positive alpha values represent potential candidates for inclusion in the actively managed component of the Treynor–Black portfolio.

A positive alpha indicates that security-generated returns above those predicted by its level of systematic risk, whereas a negative alpha suggests underperformance relative to market expectations. Consequently, securities exhibiting positive alpha values represent potential candidates for inclusion in the actively managed component of the Treynor–Black portfolio.

The results depicted in Table 5 reveal substantial variation in abnormal performance across constituent firms. Spotify Technology SA recorded the highest alpha coefficient ($\alpha = 0.003552$), followed by CTS Eventim AG & Co. KGaA ($\alpha = 0.001008$), Tele2 AB Class B ($\alpha = 0.001003$), Deutsche Telekom AG ($\alpha = 0.000837$), Publicis Groupe SA ($\alpha = 0.000802$), and Scout24 SE ($\alpha = 0.000755$). These firms demonstrated the strongest abnormal return potential during the portfolio formation period and therefore represent attractive candidates for active portfolio construction. Conversely, several firms generated negative alpha values, including Telecom Italia S.p.A. ($\alpha = -0.001020$), Infrastructure Wireless Italiane S.p.A. ($\alpha = -0.000730$), Orange SA ($\alpha = -0.000730$), Vodafone Group PLC ($\alpha = -0.000640$), Cellnex Telecom SA ($\alpha = -0.000640$), Swisscom AG ($\alpha = -0.000290$), Telefónica SA ($\alpha = -0.000150$), and Bolloré SE ($\alpha = -0.000035$). These results indicate that their observed returns fell below those predicted by their systematic risk profiles during the estimation period.

Table 5. Alpha coefficients (α) of the benchmark ETF constituents during the portfolio formation period (2024).

Asset/Company	Alpha (α)	Asset/Company	Alpha (α)
SPDR® MSCI Europe Communication Services UCITS ETF	–	Publicis Groupe SA	0.000802
Auto Trader Group PLC	0.000129	Scout24 SE	0.000755
Bolloré SE	–0.000035	Spotify Technology SA	0.003552
BT Group plc	0.000430	Swisscom AG	–0.000290
Cellnex Telecom SA	–0.000640	Tele2 AB Class B	0.001003
CTS Eventim AG & Co. KGaA	0.001008	Telecom Italia S.p.A.	–0.001020
Deutsche Telekom AG	0.000837	Telefónica SA	–0.000150
Elisa Oyj Class A	0.000019	Telenor ASA	0.000213
Informa PLC	0.000299	Telia Company AB	0.000210
Infrastrutture Wireless Italiane S.p.A.	–0.000730	Universal Music Group NV	0.000143
Koninklijke KPN NV	0.000262	Vodafone Group PLC	–0.000640
Orange SA	–0.000730	WPP PLC	0.000335

Source: Author’s calculations based on daily trading data for firms included in the MSCI Europe Communication Services 35/20 Capped Index during the portfolio formation period.

From a portfolio optimisation perspective, the findings provide strong support for active security selection. The wide dispersion in alpha values suggests that constituent firms do not contribute equally to portfolio performance and that abnormal return opportunities exist within the European communication services sector. Accordingly, the alpha estimates provide a critical input for the Treynor–Black optimisation process by identifying securities with superior risk-adjusted return potential for inclusion in the active portfolio.

4.4. Portfolio Construction Using the Treynor–Black Framework

4.4.1. Security Screening and Classification of Securities

Following the estimation of beta and alpha coefficients, all constituent firms were ranked according to their beta values, and they were classified into two equal groups: The first group includes securities with high beta, while the second group includes securities with low beta.

This classification represents an important stage of the proposed portfolio optimisation framework because it allows portfolio composition to be aligned with anticipated market conditions. Table 6 presents the classification of all constituent firms according to their systematic risk (beta) and abnormal performance (alpha). The first group comprises 11 high-beta securities that exhibit greater sensitivity to market movements and are therefore expected to perform relatively well during periods of favourable market conditions. The second group consists of 12 low-beta securities characterised by lower exposure to systematic risk and greater defensive characteristics during periods of market uncertainty.

Based on future market trends, one of two groups is selected to form the active portfolio. Assets from the first group are chosen if market trends are optimistic, and vice versa.

Based on analyses by economic and financial experts, the future trend for 2025 for the MSCI Europe Communication Services 35/20 Capped Index is positive, with the index likely to experience modest and stable growth throughout 2025.

Given the positive market outlook for the European communication services sector, attention is focused on the high-beta securities identified in Table 6. These firms were ranked according to their alpha value and the six securities with the highest positive alphas were selected for inclusion in the active portfolio. This approach reflects the central objective of the Treynor–Black model: identifying securities capable of generating returns above those predicted by their market risk exposure.

The results reveal substantial variation in both beta and alpha coefficients across constituent firms. Among the high-beta securities, Spotify Technology SA ($\alpha = 0.003552$), CTS Eventim AG & Co. KGaA ($\alpha = 0.001008$), and Scout24 SE ($\alpha = 0.000755$) generated the strongest abnormal returns, suggesting significant potential for active portfolio inclusion. In contrast, Vodafone Group PLC and Telecom Italia S.p.A. recorded negative alpha values despite their high market sensitivity, indicating weaker risk-adjusted performance. Within the low-beta group, Tele2 AB Class B ($\alpha = 0.001003$), Deutsche Telekom AG ($\alpha = 0.000837$), and Publicis Groupe SA ($\alpha = 0.000802$) demonstrated strong abnormal performance while maintaining relatively low exposure to market risk. These characteristics suggest that attractive investment opportunities may exist even among more defensive securities.

The combined analysis of beta and alpha provides a more comprehensive assessment of investment attractiveness than either measure in isolation. The findings support the application of the Treynor–Black optimisation framework, which seeks to identify securities capable of generating superior risk-adjusted returns while maintaining an appropriate balance between market exposure and firm-specific performance. This classification subsequently forms the basis for selecting the active portfolio under the expected positive market outlook for the European communication services sector.

Table 6. Classification of constituent firms based on Beta and Alpha coefficients.

Group	Asset/Company	Beta (β)	Alpha (α)
High-Beta	Vodafone Group PLC	1.450587	−0.000640
High-Beta	BT Group plc	1.204983	0.000430
High-Beta	Telecom Italia S.p.A.	1.166984	−0.001020
High-Beta	Auto Trader Group PLC	0.974542	0.000129
High-Beta	Telefónica SA	0.853639	−0.000150
High-Beta	CTS Eventim AG & Co. KGaA	0.762596	0.001008
High-Beta	Scout24 SE	0.748554	0.000755
High-Beta	Orange SA	0.732181	−0.000730
High-Beta	Spotify Technology SA	0.518134	0.003552
High-Beta	Koninklijke KPN NV	0.499074	0.000262
High-Beta	Cellnex Telecom SA	0.499549	−0.000640
Low-Beta	Swisscom AG	0.479947	−0.000290
Low-Beta	Bolloré SE	0.448476	−0.000035
Low-Beta	Deutsche Telekom AG	0.423818	0.000837
Low-Beta	Telia Company AB	0.405644	0.000210
Low-Beta	WPP PLC	0.256905	0.000335
Low-Beta	Infrastructure Wireless Italiane S.p.A.	0.243555	−0.000730
Low-Beta	Informa PLC	0.211934	0.000299
Low-Beta	Publicis Groupe SA	0.089619	0.000802
Low-Beta	Telenor ASA	0.083701	0.000213
Low-Beta	Tele2 AB Class B	−0.041770	0.001003
Low-Beta	Elisa Oyj Class A	−0.075020	0.000019
Low-Beta	Universal Music Group NV	−0.127943	0.000143

Source: Author's calculations based on daily trading data for constituent firms included in the MSCI Europe Communication Services 35/20 Capped Index during the portfolio formation period (9 January 2024–30 December 2024).

4.4.2. Selection of Securities for the Active Portfolio

Following the classification of constituent firms according to their beta and alpha characteristics, the next stage involved selecting securities for inclusion in the actively managed portfolio. Consistent with the Treynor–Black optimisation framework, security selection was based primarily on alpha coefficients, which measure abnormal returns after controlling for systematic market risk. Given the positive market outlook for the European communication services sector, attention focused on the high-beta securities identified in Table 6. These firms were ranked according to their alpha values, and the six securities with the highest positive alphas were selected for inclusion in the active portfolio. This approach reflects the central objective of the Treynor–Black model: identifying securities capable of generating returns above those predicted by their market risk exposure. The results of the selection process are presented in Table 7.

As shown in Table 7, Spotify Technology SA recorded the highest alpha coefficient among all securities included in the high-beta group, indicating the strongest abnormal return performance during the portfolio formation period. CTS Eventim AG & Co. KGaA and Scout24 SE also generated substantial positive alpha values, suggesting considerable potential for excess return generation after accounting for systematic risk. Together with BT

Group plc, Koninklijke KPN NV, and Auto Trader Group PLC, these firms demonstrated the most favourable combination of market sensitivity and abnormal return potential within the high-beta category. The selected portfolio also reflects the diversity of business models operating within the European communication services sector. The portfolio includes digital platform and streaming services (Spotify Technology SA), entertainment and event management services (CTS Eventim AG & Co. KGaA), digital marketplace businesses (Scout24 SE and Auto Trader Group PLC), telecommunications services (BT Group plc), and communication network infrastructure services (Koninklijke KPN NV). This composition provides exposure to multiple sources of value creation associated with digital transformation, platform-based business models, digital ecosystems, and next-generation communication technologies.

Table 7. Securities selected for the active portfolio.

Asset/Company	Beta (β)	Alpha (α)
Spotify Technology SA	0.518134	0.003552
CTS Eventim AG & Co. KGaA	0.762596	0.001008
Scout24 SE	0.748554	0.000755
BT Group plc	1.204983	0.000430
Koninklijke KPN NV	0.499074	0.000262
Auto Trader Group PLC	0.974542	0.000129

Source: Author's calculations based on the Treynor–Black security selection procedure.

From an international portfolio optimisation perspective, the selected securities combine strong abnormal return potential with meaningful participation in the structural transformation of the European communication services industry. Consequently, the active portfolio is positioned to capture both firm-specific performance opportunities and broader sectoral growth dynamics. These securities subsequently form the basis for the Treynor–Black optimisation procedure, through which optimal portfolio weights and the allocation between the active portfolio and the benchmark ETF are determined.

4.4.3. Estimation of Residual Variance and Determination of Active Portfolio Weights

Following the selection of the six securities constituting the active portfolio, the next stage of the Treynor–Black optimisation process involves estimating the residual variance for each selected security. Residual variance represents the unsystematic component of risk that cannot be explained by movements in the market portfolio. Within the Treynor–Black framework, this measure plays a critical role because securities with higher abnormal returns and lower residual risk receive larger portfolio weights.

The residual variance for each security is calculated using the following equation:

$$[\sigma^2(\varepsilon_i) = \sigma^2(i) - \beta_i^2 \sigma^2(m)]$$

where

$(\sigma^2(\varepsilon_i))$ = residual variance (unsystematic risk) of security (i);

$(\sigma^2(i))$ = total variance of security (i);

(β_i) = beta coefficient of security (i);

$(\sigma^2(m))$ = variance of the market portfolio represented by the benchmark ETF.

The calculation separates firm-specific risk from systematic market risk and enables the identification of securities that generate abnormal returns efficiently relative to their residual risk exposure.

As reported in Table 8, noticeable differences exist in the residual risk characteristics of the selected securities. Spotify Technology SA exhibits the highest residual variance (0.000585), indicating relatively high firm-specific volatility. This result is not unexpected given Spotify's business model, which operates within highly dynamic digital streaming and platform markets characterised by rapid technological change, evolving consumer preferences, and intense competitive pressures. While the company generated the highest alpha among all securities included in the analysis, it also exhibits the highest level of unsystematic risk.

Table 8. Residual Variance Estimates for the Selected Active Portfolio Securities.

Asset/Company	Residual Variance ($\sigma^2(\epsilon_i)$)
Spotify Technology SA	0.000585031
CTS Eventim AG & Co. KGaA	0.000329000
Scout24 SE	0.000121480
BT Group plc	0.000363155
Koninklijke KPN NV	0.000118260
Auto Trader Group PLC	0.000226473

Source: Author's calculations based on daily trading data during the portfolio formation period (9 January 2024–30 December 2024).

BT Group plc (0.000363) and CTS Eventim AG & Co. KGaA (0.000329) also display relatively high residual variance values. These results suggest that firm-specific factors, including operational performance, strategic decisions, competitive positioning, and sector-specific developments, play an important role in explaining their return behaviour beyond general market movements.

In contrast, Scout24 SE (0.000121) and Koninklijke KPN NV (0.000118) exhibit the lowest residual variance values among the selected securities. These findings indicate comparatively lower levels of firm-specific risk and suggest that their return patterns are more stable relative to the other securities included in the active portfolio. From a portfolio optimisation perspective, such firms may be particularly attractive because they combine positive alpha values with relatively low residual risk exposure.

Auto Trader Group PLC occupies an intermediate position with a residual variance of 0.000226473. While its firm-specific risk exceeds that of Scout24 SE and Koninklijke KPN NV, it remains substantially lower than that of Spotify Technology SA, BT Group plc, and CTS Eventim AG & Co. KGaA. The results presented in Table 8 highlight the importance of considering both abnormal returns and residual risk when constructing an optimal portfolio. Within the Treynor–Black model, securities are not selected solely because they generate positive alpha values. Instead, investment decisions are based on the relationship between alpha and residual variance. Securities capable of generating high abnormal returns while maintaining relatively low firm-specific risk are expected to contribute most effectively to portfolio performance. From the perspective of international portfolio optimisation in a digitally transforming sector, these findings demonstrate that digital growth opportunities are often accompanied by differing levels of firm-specific risk. Consequently, the Treynor–Black framework provides an appropriate mechanism for balancing return enhancement against residual risk exposure, thereby supporting the construction of an efficient and internationally diversified portfolio within the European communication services sector.

4.4.4. Determination of Active Portfolio Weights

A fundamental feature of the Treynor–Black optimisation framework is that portfolio weights are determined according to the relationship between a security’s abnormal return (alpha) and its residual variance. This approach ensures that portfolio allocations reflect both return-generating potential and firm-specific risk exposure. Securities generating higher abnormal returns relative to their residual risk receive larger portfolio weights and therefore contribute more significantly to overall portfolio performance.

The relative attractiveness of each security is measured using the alpha-to-residual variance ratio:

$$\left[\frac{\alpha_i}{\sigma^2(\varepsilon_i)}\right]$$

where

α_i represents the abnormal return (alpha) of security i ;

$\sigma^2(\varepsilon_i)$ denotes the residual variance of security i .

This ratio measures the amount of abnormal return generated per unit of unsystematic risk. Higher values indicate superior risk-adjusted abnormal performance and justify a greater allocation within the active portfolio.

Following the calculation of the alpha-to-residual variance ratios, the optimal weight assigned to each security within the active portfolio is determined as follows:

$$W_i = \frac{\alpha_i / \sigma^2(\varepsilon_i)}{\sum_{i=1}^n \alpha_i / \sigma^2(\varepsilon_i)}$$

where W_i represents the proportion of the active portfolio allocated to security i .

This procedure ensures that securities exhibiting stronger abnormal return performance relative to residual risk receive proportionally larger allocations. Consequently, the resulting portfolio weights reflect each security’s contribution to the expected risk-adjusted performance of the active portfolio.

The results reveal substantial variation in the risk-adjusted abnormal performance of the selected securities. Scout24 SE recorded the highest alpha-to-residual variance ratio (6.218), closely followed by Spotify Technology SA (6.072), indicating that both firms generated exceptional abnormal returns relative to their levels of firm-specific risk. Consequently, these securities receive the largest allocations within the active portfolio, accounting for approximately 32.17% and 31.14% of portfolio value, respectively.

CTS Eventim AG & Co. KGaA also demonstrates strong performance, with a ratio of 3.064 and an allocation of 15.9%. Similarly, Koninklijke KPN NV achieves a favourable balance between abnormal return generation and residual risk, resulting in a portfolio weight of 11.5%. By contrast, BT Group plc and Auto Trader Group PLC receive smaller allocations because their abnormal returns are comparatively modest when evaluated relative to firm-specific risk.

From an international portfolio optimisation perspective, these findings highlight the importance of jointly evaluating return potential and residual risk rather than focusing solely on expected returns. The results indicate that firms operating in digitally enabled business segments, including digital platforms, online marketplaces, and technology-driven communication services, demonstrate particularly attractive risk-adjusted abnormal performance. This observation is consistent with the broader digital transformation trends characterising the European communication services sector and reinforces the value of active security selection within innovation-intensive industries.

The allocation structure presented in Table 9 reflects the central logic of the Treynor–Black model: capital is directed towards securities capable of generating superior abnormal returns while maintaining efficient control over firm-specific risk. These weights subse-

quently form the basis for constructing the active portfolio and determining the optimal allocation between active and passive investments.

Table 9. Risk-Adjusted Abnormal Performance and Optimal Active Portfolio Weights under the Treynor–Black Framework.

Asset/Company	Alpha-to-Residual Variance Ratio ($(\alpha_i / \sigma^2(\varepsilon_i))$)	Active Portfolio Weight (W_i)
Spotify Technology SA	6.072082	0.314167
CTS Eventim AG & Co. KGaA	3.064006	0.158530
Scout24 SE	6.217777	0.321705
BT Group plc	1.183984	0.061258
Koninklijke KPN NV	2.217382	0.114726
Auto Trader Group PLC	0.517499	0.029611
Total	–	1.000000

Source: Author's calculations based on the Treynor–Black optimisation framework.

After calculating the weight of each asset within the active diversified portfolio, the following is calculated:

$$\alpha_A = \sum_{i=1}^n W_i \cdot \alpha_i$$

which gives $\alpha_A = 0.001579154$.

Calculating the unsystematic risk of an active diversified portfolio through the relationship:

$$\sigma^2(\varepsilon_A) = \sum_{i=1}^n W_i^2 \cdot \sigma^2(\varepsilon_i)$$

which gives $\sigma^2(\varepsilon_A) = 0.0000817049$.

Beta account, a diversified wallet active through the relationship

$$\beta_A = \sum_{i=1}^n W_i \cdot \beta_i$$

gives $\beta_A = 0.684419827$.

Calculating the relationship

$$W_A^0 = \frac{\frac{\alpha_A}{\sigma^2(\varepsilon_A)}}{\frac{E(R_m)}{\sigma^2(m)}}$$

gives $W_A^0 = 1.534422594$.

Calculating the weight of the diversified active portfolio within the investment portfolio

$$W_A = \frac{W_A^0}{1 + (1 - \beta_A)W_A^0}$$

gives $W_A = 1.03381493$.

Calculating the weight of an index fund portfolio within an investment portfolio

$$W_m = 1 - W_A$$

gives $W_m = 1 - 1.03381493 = -0.03381493$.

That is, the benchmark index should be sold short (short sale).

Forming the proposed optimal investment portfolio

$$W_P = W_A + W_m$$

Building the proposed optimal investment portfolio according to the Treynor–Black approach: Based on the weights calculated according to the Treynor–Black model for each asset, the weight of the diversified active portfolio will be weighted by the calculated asset weight.

Building the proposed optimal investment portfolio according to the equal-weight approach: Using this method, the researcher will distribute the active diversified portfolio equally among the portfolio’s assets. Therefore,

$$\text{Asset weight within the investment portfolio} = \frac{\text{Active diversified portfolio weight}}{\text{Number of assets}} = \frac{1.03381493}{6} = 0.1723024$$

The allocation structure presented in Table 10 highlights the key differences between the Treynor–Black optimisation framework and a naïve equal-weight strategy.

Table 10. Active diversified portfolio asset weights within an optimal investment portfolio according to Treynor–Black.

Asset/Company	Active Portfolio Weight (W_i)	Percentage of Active Diversified Portfolio in the Investment Portfolio (W_A)	Asset Weight Within an Optimal Investment Portfolio
Spotify Technology SA	0.314167	1.03381493	0.324790849
CTS Eventim AG & Co. KGaA	0.158530	1.03381493	0.163891226
Scout24 SE	0.321705	1.03381493	0.33258395
BT Group plc	0.061258	1.03381493	0.063330377
Koninklijke KPN NV	0.114726	1.03381493	0.118605977
Auto Trader Group PLC	0.029611	1.03381493	0.030612551

Source: Author’s calculations based on the Treynor–Black optimisation framework.

As shown in Table 11, Under the Treynor–Black approach, portfolio weights are determined by each security’s risk-adjusted abnormal return potential, resulting in a concentrated allocation towards firms exhibiting the most favourable alpha-to-risk characteristics. Consequently, Spotify Technology SA and Scout24 SE receive substantially larger portfolio weights than under the equal-weight approach, reflecting their superior ability to generate abnormal returns relative to firm-specific risk. By contrast, the equal-weight portfolio allocates identical weights to all selected securities irrespective of differences in expected performance or risk characteristics. These contrasting allocation strategies provide an appropriate basis for evaluating whether active portfolio optimisation can create additional value beyond simple diversification. More importantly, the Treynor–Black portfolio exhibits greater exposure to firms benefiting from digital transformation, platform-based business models, data-driven innovation, and technology-enabled growth opportunities, while maintaining broad market exposure through the benchmark ETF. The subsequent performance analysis therefore examines whether this optimisation strategy translates into superior return generation and risk-adjusted performance during the evaluation period.

Table 11. Comparison of Portfolio Allocations under the Treynor–Black and Equal-Weight Approaches.

Asset/Company	Treynor–Black Portfolio	Equal-Weight Portfolio
Spotify Technology SA	0.324790849	0.1723024
CTS Eventim AG & Co. KGaA	0.163891226	0.1723024
Scout24 SE	0.33258395	0.1723024
BT Group plc	0.063330377	0.1723024
Koninklijke KPN NV	0.118605977	0.1723024
Auto Trader Group PLC	0.030612551	0.1723024
SPDR [®] MSCI Europe Communication Services UCITS ETF	−0.03381493	−0.03381493
Total	1.000000	1.000000

Source: Author’s calculations.

4.5. Portfolio Performance Evaluation

Following portfolio construction, the performance of the proposed portfolios was evaluated over the out-of-sample period from 6 January 2025 to 7 October 2025. Consistent with the objectives of this study, portfolio performance was assessed using both return-based and risk-adjusted measures, enabling an evaluation of whether active portfolio optimisation generates superior investment outcomes within the European communication services sector. Detailed return calculations, portfolio beta estimations, and risk-adjusted performance measures are reported in Appendices A–D: Appendix A (returns), Appendix B (beta), Appendix C (risk estimation), and Appendix D (risk-adjusted performance).

Portfolio returns were calculated as:

$$\bar{R}_P = \sum_{i=1}^n W_i \bar{R}_i$$

where (W_i) represents the portfolio weight of security (i), and ($\bar{R}_i$) denotes its average return during the evaluation period.

As reported in Table 12, the Treynor–Black portfolio generated a higher average daily return (0.0010931) than the equal-weight portfolio (0.000843). When annualised, these returns correspond to 27.3% and 21.09%, respectively. Meanwhile, the market benchmark index achieved an average daily return (0.000). The superior performance of the Treynor–Black portfolio suggests that active security selection contributed positively to return generation during the evaluation period and supports the argument that optimisation techniques can enhance portfolio returns within a digitally transforming sector. However, return performance alone provides an incomplete assessment of portfolio effectiveness because higher returns may be accompanied by greater levels of risk. Consequently, both portfolios were further evaluated using beta, standard deviation, the Sharpe ratio, and the Treynor ratio to assess performance relative to total and systematic risk.

Table 12. Portfolio return comparison: Treynor–Black and Equal-Weight Portfolios.

Portfolio	Average Daily Return	Annualised Return
Treynor–Black Portfolio	0.0010931	0.2732
Equal-Weight Portfolio	0.000843	0.21094
Benchmark ETF	0.000627	0.156778

Source: Author’s calculations. The detailed security-level return contributions underlying the portfolio return calculations are reported in Appendix A.

The results presented in Table 12 reveal a clear trade-off between return maximisation and risk-adjusted performance. Consistent with the findings reported in Table 12, the Treynor–Black portfolio generated the highest annual return (27.3%). As shown in Table 11, the portfolio also maintained a beta close to unity (0.9848), indicating market-level systematic risk exposure. Furthermore, the positive Sharpe ratio (1.2159) and Treynor ratio (0.2572) indicate that the portfolio generated returns above the risk-free rate after accounting for both total and systematic risk.

By contrast, Table 13 shows that the equal-weight portfolio exhibited lower systematic risk ($\beta = 0.695225$) and lower overall volatility ($\sigma = 0.1684$) than the Treynor–Black portfolio. Although its annual return was lower, the portfolio achieved superior Sharpe (1.1337) and Treynor (0.27464) ratios. The evidence presented in Tables 12 and 13 indicates that the Treynor Black portfolio achieved a higher annualized return than the equal-weighted portfolio and a higher Sharpe ratio, While the equal-weighted portfolio achieved a higher Treynor ratio which constitutes empirical evidence supporting the hypothesis test result.

Table 13. Comparative risk and risk-adjusted performance of the proposed portfolios.

Performance Measure	Treynor–Black Portfolio	Equal-Weight Portfolio	Benchmark ETF
Annual Return	0.2732	0.21094	0.1567
Portfolio Beta	0.984823	0.695225	1
Annualized Standard Deviation	0.20831021	0.168414636	0.1586
Sharpe Ratio	1.21596	1.13376	0.8619
Treynor Ratio	0.257201	0.27464	0.1367

Source: Author’s calculations. The calculations supporting portfolio beta, standard deviation, Sharpe ratio, and Treynor ratio are presented in Appendices B–D.

The evidence reported in Tables 12 and 13 indicates that active portfolio optimisation enhanced absolute return performance, whereas the equal-weight strategy delivered stronger risk-adjusted performance, according to the Trainor Index. The findings therefore highlight the importance of balancing return enhancement with diversification efficiency when constructing international portfolios within digitally transforming sectors. While active optimisation may improve return generation, superior absolute returns do not necessarily translate into superior risk-adjusted outcomes, these results provide the empirical foundation for the formal hypothesis testing presented in the following section.

The comparison reveals that the Treynor–Black portfolio generated the highest absolute return, whereas the equal-weight portfolio achieved superior risk-adjusted performance. Specifically, the higher Treynor ratio of the equal-weight portfolio suggest that its diversification benefits outweighed the return advantages associated with active optimisation. These findings indicate that while active portfolio management can enhance return generation within a digitally transforming sector, simple diversification strategies may provide superior performance when evaluated on a risk-adjusted basis. This result offers important insights for investors seeking exposure to firms operating within Europe’s evolving digital communication ecosystem and provides the basis for the formal hypothesis testing presented in the following section.

4.6. Hypothesis Testing Results

This section evaluates whether the proposed Treynor–Black portfolio generated performance that differed significantly from both the equal-weight portfolio and the benchmark ETF portfolio. The analysis was conducted using paired-samples *t*-tests based on daily portfolio returns during the evaluation period (6 January 2025–7 October 2025).

4.6.1. Treynor–Black Portfolio Versus Equal-Weight Portfolio

The first hypothesis examines whether the Treynor–Black optimisation framework produced performance significantly different from the equal-weight portfolio.

H1a. *There is no statistically significant difference between the performance (measured according to the Sharpe index) of the Treynor–Black portfolio and the equal-weight portfolio.*

As reported in Table 14, the Treynor–Black portfolio generated a higher average Sharpe index than the equal-weight portfolio but also exhibited greater volatility. Therefore, the risk-adjusted portfolio performance using the Treynor–Black approach is better than the portfolio performance using the equal-weighted approach.

Table 14. Descriptive Statistics of Sharpe Portfolio index.

Portfolio	Mean	N	Std. Deviation	Std. Error Mean
Treynor–Black Portfolio	1.21596524	194	15.81138830	1.135191523
Equal-Weight Portfolio	1.13376551	194	15.81138830	1.135191523

Source: Author’s calculations.

The results shown in Table 15 indicate that the mean difference between the Sharpe value for the first and second portfolios is 0.082199734, the standard deviation of the mean difference is 9.298385106, and the test statistic value is 0.123. Since the test statistic falls within the 95% confidence interval, the null hypothesis cannot be rejected; that is, there are no substantial differences in risk-adjusted performance between the first portfolio according to the Treynor–Black approach and the equal-weighted approach.

Table 15. Paired-Samples *t*-Test: Treynor–Black versus Equal-Weight Portfolio.

Mean	Std. Deviation	Std. Error Mean	95% Confidence Interval of the Difference		t	df	Sig. (2-Tailed)
			Lower	Upper			
0.082199734	9.298385106	0.667585145	−1.234499594	1.398899061	0.123	193	0.902

Source: Author’s calculations.

4.6.2. Proposed Portfolio Versus Benchmark ETF Portfolio

The second hypothesis examines whether the proposed Treynor–Black portfolio outperformed the benchmark market portfolio represented by the SPDR® MSCI Europe Communication Services UCITS ETF.

H2a. *There is no statistically significant difference between the performance of the proposed portfolio and the benchmark European communication services market portfolio.*

The results shown in Table 16 demonstrate the superiority of the proposed optimal portfolio based on the Treynor–Black approach over the market index portfolio based on the Sharpe value. The proposed optimal portfolio achieved a positive Sharpe value of 1.21596524, while the Sharpe value for the market portfolio was 0.86194277.

The results shown in Table 17 indicate that the mean difference between the Sharpe value for the first and second portfolios is 0.354022470, the standard deviation of the mean difference is 1.114644423E1, and the test statistic value is 0.442. Since the test statistic falls within the 95% confidence interval, the null hypothesis cannot be rejected; that is, there are no substantial differences in risk-adjusted performance between the first portfolio

according to the Treynor–Black approach and the benchmark European communication services market portfolio.

Table 16. Descriptive Statistics of Sharpe Portfolio index.

Portfolio	Mean	N	Std. Deviation	Std. Error Mean
Treynor–Black Portfolio	1.21596524	194	15.81138830	1.135191523
benchmark European communication services market portfolio	0.86194277	194	15.85229752	1.138128634

Source: Author’s calculations.

Table 17. Paired-Samples *t*-Test: Treynor–Black versus benchmark Portfolio.

Mean	Std. Deviation	Std. Error Mean	95% Confidence Interval of the Difference		t	df	Sig. (2-Tailed)
			Lower	Upper			
0.354022470	11.14644423	0.800268057	−1.224371568	1.932416509	0.442	193	0.659

Source: Author’s calculations.

5. Discussion of the Results: The Influence of Digital Transformation and Governance Quality on International Portfolio Optimisation

The findings of this study demonstrate that international portfolio optimisation within the European communication services sector should be interpreted within a broader ecosystem characterised by digital transformation, governance quality, innovation capability, and institutional effectiveness. While the empirical analysis focused on portfolio construction using the Treynor–Black optimisation framework, the results indicate that investment performance is influenced not only by firm-level financial characteristics but also by the digital and institutional environments in which firms operate. The European communication services sector provides a particularly relevant setting for this analysis because it operates at the intersection of technological innovation, digital infrastructure development, artificial intelligence adoption, platform-based business models, and rapidly evolving consumer demand. Notably, the portfolio is concentrated in comparatively digitally developed and institutionally stable European economies, yet this study does not empirically test the association between these contextual characteristics and portfolio performance.

The portfolio optimisation results provide important insights into the effectiveness of active portfolio management within this environment. The proposed Treynor–Black portfolio generated the highest annual return (27.3%), outperforming both the benchmark ETF portfolio and the equal-weight portfolio. Furthermore, the results of the hypothesis testing revealed no statistically significant difference in the Sharpe value between the proposed portfolio and the market portfolio. These findings suggest that investors may be able to generate superior returns by actively identifying securities with favourable abnormal return characteristics rather than relying solely on passive exposure to sector-wide market indices. Consequently, the results support the central proposition of this study that international portfolio optimisation can create value within sectors undergoing rapid technological and digital transformation.

At the same time, the findings highlight the continuing importance of diversification and risk management. Although the Treynor–Black portfolio generated superior absolute returns, the equal-weight portfolio achieved higher Treynor ratios, indicating stronger risk-adjusted performance. Moreover, the difference between the Treynor–Black portfolio and the equal-weight portfolio was not statistically significant ($p > 0.05$). This result suggests that while active portfolio optimisation can enhance return generation, diversification

remains a critical determinant of portfolio efficiency. The findings therefore reinforce a key principle of Modern Portfolio Theory (Markowitz, 1952): superior portfolio performance depends not only on return maximisation but also on the effective management of risk through diversification.

The digital transformation indicators presented in Figure 3 further help explain the sector's investment attractiveness. Several countries represented within the benchmark portfolio, particularly Germany, Luxembourg, the United Kingdom, and France, rank among Europe's most digitally advanced economies. High levels of digital maturity support technology adoption, innovation ecosystems, digital infrastructure, and advanced connectivity services. These conditions create favourable environments for communication service firms operating in digital platforms, cloud computing, AI, cybersecurity, data analytics, and next-generation telecommunications. As a result, digital transformation functions as an important driver of corporate growth, competitiveness, and long-term value creation, ultimately influencing portfolio-level performance.

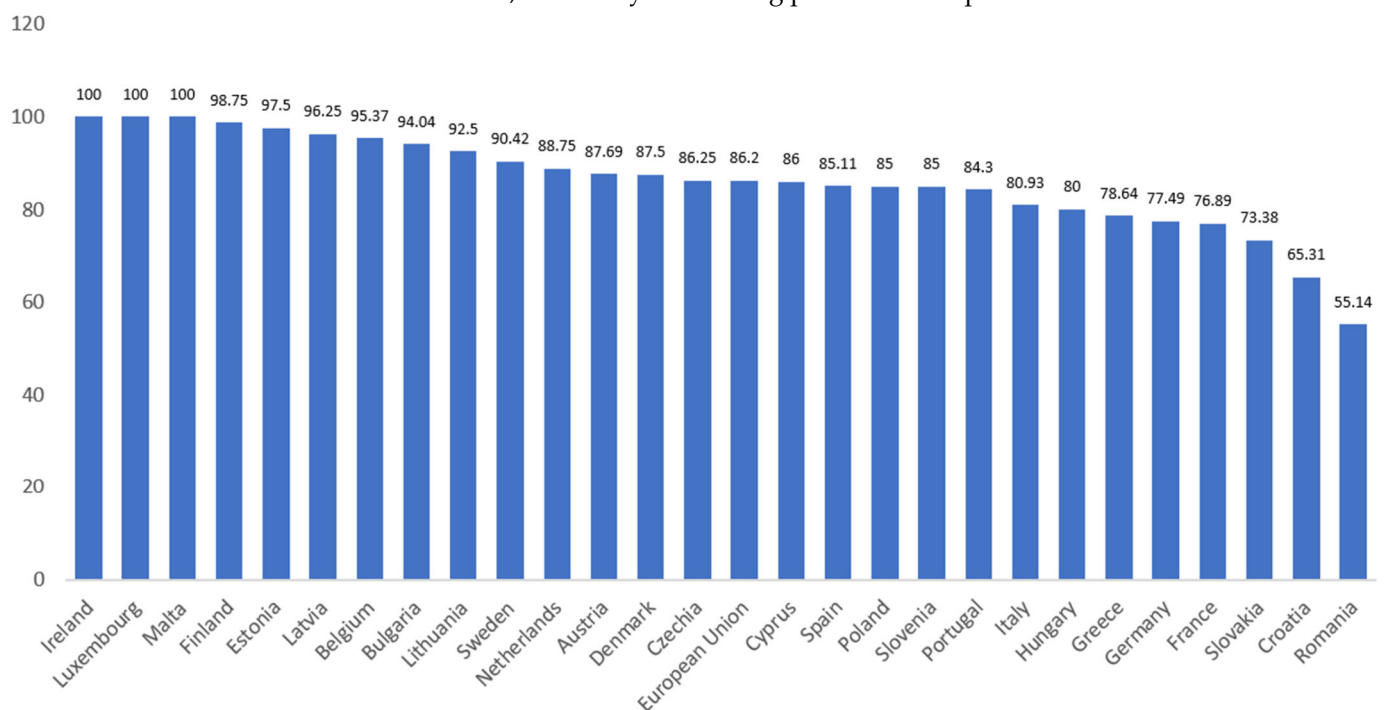


Figure 3. Digital Economy and Society Index (DESI) Scores Across European Countries (2024). Source: DESI (2024).

Governance quality further reinforces the sector's investment attractiveness. As illustrated in Figure 4, the principal countries within the benchmark portfolio demonstrate strong performance across key governance dimensions, including government effectiveness, regulatory quality, rule of law, accountability, and institutional stability. Such environments reduce uncertainty, strengthen investor protection, enhance transparency, and support efficient capital allocation, factors particularly important in digitally transforming sectors requiring continuous investment in technological infrastructure and innovation capabilities. Prior studies demonstrate that firms within advanced digital ecosystems and robust governance structures are better positioned to convert technological investments into sustainable competitive advantage. Furthermore, Alkaraan et al. (2026) show that digital transformation strengthens organisational agility and corporate resilience under conditions of technological disruption and market uncertainty. Collectively, these studies suggest that governance quality and digital transformation operate as complementary drivers of competitiveness, resilience, and long-value creation. More broadly, the findings suggest

that successful international portfolio optimisation should not rely exclusively on traditional financial indicators such as return, beta, or volatility. Investors should also consider country-level digital competitiveness, governance effectiveness, innovation ecosystems, and institutional quality when evaluating investment opportunities. In this respect, digital transformation and governance quality emerge as complementary drivers of portfolio performance, influencing growth opportunities, risk characteristics, and investment resilience.

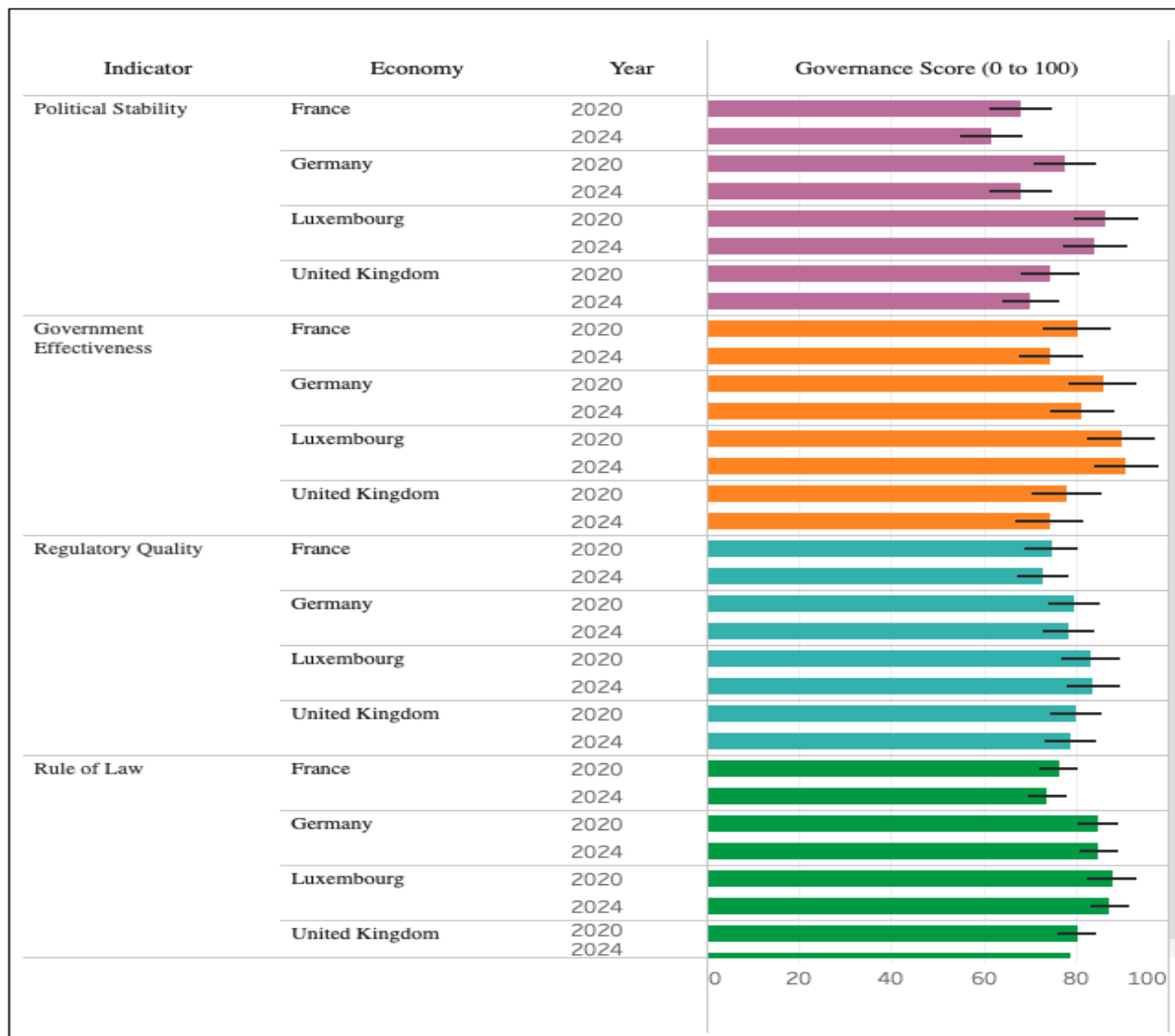


Figure 4. Selected Worldwide Governance Indicator Scores for Major Portfolio Countries. Source: Worldwide governance indicator, World Bank Group. <https://www.worldbank.org/en/publication/worldwide-governance-indicators/interactive-data-access> (accessed on 9 June 2026).

The results indicate that the European communication services sector offers an attractive environment for international portfolio optimisation, combining strong digital capabilities, supportive institutional frameworks, advanced innovation ecosystems, and favourable growth prospects. The evidence suggests that active portfolio management can create value within such an environment, although the benefits of active optimisation should be balanced against the diversification advantages of simpler portfolio construction approaches. Consequently, successful portfolio management in digitally transforming sectors requires an integrated approach that combines active security selection, diversifi-

cation, risk management, governance assessment, and an understanding of the broader technological forces shaping future investment performance.

Figures 3 and 4 present descriptive country-level indicators drawn from the European Commission's Digital Economy and Society Index (DESI, 2024) and the World Bank's Worldwide Governance Indicators (WGI, 2024), respectively. These indicators are presented solely for contextual interpretation of the sector's investment environment and are not intended to imply a causal relationship; their association with portfolio performance is not empirically tested in this study.

6. Conclusions

This study examined international portfolio optimisation within a digitally transforming sector, focusing on constituent firms of the MSCI Europe Communication Services 35/20 Capped Index. The communication services sector represents a particularly relevant setting for portfolio analysis, as it lies at the centre of Europe's digital transformation agenda and is increasingly shaped by artificial intelligence (AI), digital platforms, cloud computing, advanced telecommunications infrastructure, big data analytics, and technology-enabled business models. Within this context, the study developed and evaluated a Treynor–Black optimisation framework, comparing its performance with both an equal-weight portfolio and the benchmark SPDR® MSCI Europe Communication Services UCITS ETF.

The empirical findings provide important insights into the effectiveness of active portfolio management within a digitally transforming and innovation-intensive sector. The Treynor–Black portfolio achieved the highest annual return (27.3%) and outperformed the benchmark market portfolio, demonstrating the potential of active security selection to identify firms capable of generating superior returns. Furthermore, it achieved the highest Sharpe ratio (1.215) compared between an equal-weighted portfolio and a market index portfolio. However, the equal-weight portfolio generated stronger risk-adjusted performance, as evidenced by its higher Treynor ratios. Furthermore, the hypothesis testing results revealed no statistically significant difference between the performance of the Treynor–Black portfolio and the equal-weight portfolio ($p > 0.05$), indicating that the additional complexity associated with active optimization did not generate statistically superior performance relative to a simpler diversification strategy. Furthermore, the results did not show a significant difference between the performance of the Treynor–Black portfolio and the performance of the market index.

More broadly, the findings suggest that portfolio performance is influenced not only by firm-level financial characteristics but also by the wider digital and institutional environments in which firms operate. The analysis demonstrated that the benchmark portfolio is concentrated in countries such as Germany, Luxembourg, the United Kingdom, and France, which exhibit high levels of digital maturity, governance effectiveness, innovation capability, regulatory quality, and institutional stability. These characteristics create favourable conditions for communication service firms to leverage digital technologies, invest in innovation, and develop sustainable competitive advantages. Consequently, digital transformation and governance quality emerge as important contextual determinants of portfolio performance, investment resilience, and long-term value creation.

6.1. Theoretical and Managerial Implications

From a theoretical perspective, this study contributes to the international portfolio management literature by extending the Treynor–Black optimisation framework to a digitally transforming and innovation-intensive sector. Traditional portfolio optimisation studies have predominantly focused on financial variables, market risk, diversification benefits, and asset allocation decisions. In contrast, the present study demonstrates that

portfolio performance may also be influenced by broader contextual factors, including digital transformation, governance quality, institutional effectiveness, and innovation capacity. By integrating these dimensions into the discussion of portfolio performance, the study establishes an important connection between international portfolio management and the growing literature on digital transformation, governance, and value creation.

The findings are broadly consistent with prior research emphasising the strategic role of digital transformation, governance quality, and innovation capability in enhancing organisational performance and long-term value creation. Previous studies suggest that firms within advanced digital ecosystems and supported by effective governance structures are better positioned to convert technological investments into sustainable competitive advantages and superior financial performance. Recent evidence demonstrates that digital transformation enhances organisational agility and corporate resilience, strengthening firms' ability to respond to technological disruption, market uncertainty, and changing competitive conditions (Probojakti et al., 2025; Alkaraan et al., 2026).

Recent research also highlights the importance of leadership and knowledge-based capabilities in supporting innovation outcomes. Harsono et al. (2025) demonstrate that transformational leadership and knowledge management significantly influence innovation capability, which in turn enhances innovation performance. Their findings emphasise the complex interrelationships between leadership, organisational learning, knowledge creation, and innovation-driven growth. Collectively, this body of literature suggests that the benefits of digital transformation extend beyond operational efficiency to encompass broader strategic capabilities supporting innovation, adaptability, resilience, sustainable growth, and long-term value creation.

The present study extends these insights beyond the firm level to the domain of international portfolio optimisation. While previous research has primarily examined the organisational consequences of digital transformation and governance quality, this study demonstrates that these factors may also influence portfolio-level outcomes through their impact on firm performance, growth opportunities, risk characteristics, and investment attractiveness. The empirical results indicate that active portfolio optimisation can generate superior returns relative to the benchmark, while the discussion of digital maturity and governance quality suggests that firms within technologically advanced and institutionally robust environments may offer more attractive investment opportunities. Consequently, the study contributes to emerging debates concerning how digital ecosystems, governance effectiveness, and innovation-led growth influence investment performance within the digital economy.

More broadly, the findings suggest that international portfolio optimisation should not be viewed solely through the lens of traditional financial metrics. In sectors characterised by rapid technological change, investors may benefit from incorporating broader indicators relating to digital competitiveness, governance quality, innovation capability, and institutional effectiveness into portfolio construction and security selection decisions. Digital transformation and governance quality therefore emerge not only as drivers of firm-level competitiveness but also as important determinants of portfolio efficiency, risk-adjusted performance, and long-term investment value.

From a managerial perspective, the findings provide several important implications for investors, fund managers, and financial institutions. First, portfolio construction within digitally transforming sectors should incorporate assessments of digital maturity, innovation capability, governance effectiveness, and institutional quality alongside conventional financial indicators. Such considerations may assist investors in identifying firms better positioned to exploit technological opportunities and sustain long-term growth. Second, the results demonstrate that superior returns do not necessarily translate into superior

risk-adjusted performance. Although the Treynor–Black portfolio generated the highest return, the equal-weight portfolio produced stronger risk-adjusted outcomes, highlighting the continuing importance of diversification in portfolio management. Third, the findings suggest that active portfolio management can create value when combined with disciplined risk management and diversification strategies. Investors should therefore avoid excessive concentration in a small number of high-growth securities and instead seek an appropriate balance between return enhancement and portfolio stability. Finally, the study highlights the importance of country-level characteristics in international investment decision-making. Digital infrastructure, governance quality, regulatory effectiveness, innovation ecosystems, and institutional stability may all influence investment opportunities and portfolio performance. Consequently, international investors should complement firm-level financial analysis with a broader assessment of the digital and governance environments within which firms operate when making asset allocation and portfolio optimisation decisions.

6.2. Limitations and Suggestions for Future Research

Despite its contributions, this study is subject to several limitations. First, the analysis focuses exclusively on the European communication services sector and may not fully capture the dynamics of other sectors or geographic regions. Second, the evaluation period covers a specific market environment and may not reflect longer-term structural changes associated with technological disruption, economic cycles, or regulatory developments. Third, the portfolio optimisation framework relies primarily on historical market data and therefore remains subject to the limitations inherent in historical performance analysis.

Future research could extend this study in several directions. First, alternative optimisation techniques, including the Black–Litterman model, multi-factor asset pricing models, machine learning approaches, and AI-driven portfolio construction frameworks, could be compared with the Treynor–Black model. Second, future studies may explicitly integrate governance indicators, ESG metrics, digital transformation measures, and digital competitiveness indices into portfolio optimisation models to examine their direct influence on portfolio performance. Third, comparative analyses across sectors, countries, and regions would provide deeper insights into how institutional quality, governance structures, and digital maturity affect investment outcomes. Finally, future research may explore the growing role of artificial intelligence, digital governance, sustainability performance, and innovation ecosystems as emerging drivers of portfolio returns in increasingly digitalised global capital markets.

The study provides evidence that international portfolio optimisation can create value within the European communication services sector—a sector positioned at the forefront of digital transformation and technological innovation. However, the findings also demonstrate that successful portfolio management requires more than the pursuit of superior returns. Effective investment strategies must integrate active security selection, international diversification, governance quality, digital transformation considerations, and risk management. As digitalisation, artificial intelligence, and innovation continue to reshape global industries and capital markets, understanding their implications for portfolio construction and investment performance will remain an increasingly important area for both academic research and professional investment practice.

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Appendix A

Table A1. Treynor–Black portfolio return calculation.

Asset/Company	Portfolio Weight	Average Daily Return	Contribution
Spotify Technology SA	0.324790849	0.001718	0.00055
CTS Eventim AG & Co. KGaA	0.163891226	0.000714	0.0000117
Scout24 SE	0.33258395	0.001153	0.000383
BT Group plc	0.063330377	0.001101	0.0000697
Koninklijke KPN NV	0.118605977	0.000700	0.0000829
Auto Trader Group PLC	0.030612551	0.000276	0.0000084
SPDR® MSCI Europe Communication Services UCITS ETF	−0.03381493	0.000627	−0.0000210
Portfolio Return			0.00109

This appendix presents the detailed portfolio return calculations for the Treynor–Black portfolio during the evaluation period (6 January 2025–7 October 2025).

Annualised Return: $[0.00109 \times 250 = 0.273] [=27.3\%]$

Appendix B

Table A2. Treynor–Black Portfolio Beta calculations.

Security	Weight	Beta	Weighted Beta
Spotify Technology SA	0.324790849	1.805715987	0.586480028
CTS Eventim AG & Co. KGaA	0.163891226	0.656568454	0.107605809
Scout24 SE	0.33258395	0.754988074	0.251096916
BT Group plc	0.063330377	0.49992305	0.031660315
Koninklijke KPN NV	0.118605977	0.296168146	0.035127312
Auto Trader Group PLC	0.030612551	0.217806601	0.006667616
ETF	−0.03381493	1	−0.03381493
Portfolio Beta			

This appendix presents the detailed portfolio beta calculations for the Treynor–Black portfolio during the evaluation period (6 January 2025–7 October 2025).

Portfolio beta was estimated using the weighted-average beta approach:

$$\beta_P = \sum_{i=1}^n W_i \beta_i$$
, where W_i represents portfolio weight and β_i represents the beta coefficient of security (i).

Appendix C

Table A3. Portfolio risk results.

Measure	Treynor–Black	Equal-Weight
Daily Standard Deviation	0.013174694	0.010651477
Annualised Standard Deviation	0.20831021	0.168414636

Portfolio variance was estimated using the variance-covariance matrix approach: $[\sigma^2_P = W' \Sigma W]$, where $[W]$ represents the vector of portfolio weights, and $[\Sigma]$ represents the variance-covariance matrix of asset returns.
Portfolio standard deviation is calculated as: $[\sigma_P = \sqrt{\sigma^2_P}]$
The Treynor–Black portfolio exhibited higher volatility due to its greater concentration in securities with stronger abnormal return potential, whereas the Equal-Weight portfolio benefited from broader diversification.

Appendix D

Table A4. Summary of risk-adjusted performance: Sharpe Ratio and Treynor Ratio Calculations.

Measure	Treynor–Black	Equal-Weight
Sharpe Ratio	1.215965241	1.133765507
Treynor Ratio	0.257201505	0.274648447

The Treynor–Black portfolio achieved superior risk-adjusted performance, according to the Sharpe Index.
Meanwhile, the equal-weighted portfolio achieved superior risk-adjusted performance, according to the Treynor Index.
The ECB Deposit Facility Rate of approximately 2% was adopted as the risk-free rate.
Sharpe Ratio $[\text{Sharpe} = \frac{R_P - R_f}{\sigma_P}]$
Treynor–Black Portfolio $[\frac{0.273 - 0.02}{0.2083} = 1.215965241]$
Equal-Weight Portfolio $[\frac{0.210 - 0.02}{0.1684} = 1.1337]$
Treynor Ratio $[\text{Treynor} = \frac{R_P - R_f}{\beta_P}]$
Treynor–Black Portfolio $[\frac{0.273 - 0.02}{0.9848} = 0.2572]$
Equal-Weight Portfolio $[\frac{0.210 - 0.02}{0.695} = 0.2746]$

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